How many distinct triangles can you find in the graph above? What about graphs that aren't complete? One interesting solution involves associating the graph with a collection of polynomials - called the edge ideal. This association allows one to use algebra to study graphs. In this talk, we will present a hands-on approach to this field, using SAGE to compute examples and explore recent results and open problems in this area.