



### Math 305 – Introduction to Numerical Methods Course Syllabus

**Course description:** Basic numerical and computational techniques used in solution of mathematical problems in the real world: approximation of functions, roots and systems of equations, numerical integration, interpolation and curve fitting, and machine computation.

**Credit hours:** 3

**Course Prerequisites and Corequisites:** MTH 234 and CSC 102 or equivalent.

<u>Course outline:</u>	<u>Approximate time spent</u>
<ul style="list-style-type: none"><li>● <b>Equations in One Variable</b><ul style="list-style-type: none"><li>○ Background<ul style="list-style-type: none"><li>▪ Calculus Review</li><li>▪ Roundoff Error and Computer Arithmetic</li><li>▪ Convergence, Algorithms and Computer Software</li></ul></li><li>○ Numeric Solution Methods<ul style="list-style-type: none"><li>▪ Bisection, Secant, and Newton's methods</li><li>▪ Error analysis and Accelerating convergence</li><li>▪ Other methods for polynomials</li></ul></li></ul></li></ul>	30%
<ul style="list-style-type: none"><li>● <b>Interpolation and Polynomial Approximation</b><ul style="list-style-type: none"><li>○ Interpolation and the Lagrange method</li><li>○ Divided differences</li><li>○ Hermite Polynomials</li><li>○ Spline interpolation</li><li>○ Parametric curves</li></ul></li></ul>	20%
<ul style="list-style-type: none"><li>● <b>Numerical Differentiation and Integration</b><ul style="list-style-type: none"><li>○ Numerical differentiation</li><li>○ Numerical Integration<ul style="list-style-type: none"><li>▪ Basic and composite quadratures</li><li>▪ Other methods; Romberg, Gaussian, Adaptive</li><li>▪ Multiple and Improper integrals</li></ul></li></ul></li></ul>	25%
<ul style="list-style-type: none"><li>● <b>Numeric methods for Systems of Equations</b><ul style="list-style-type: none"><li>○ Linear Systems<ul style="list-style-type: none"><li>▪ Norms of vectors and matrices</li><li>▪ Eigenvalues and eigenvectors</li><li>▪ Jacobi, Gauss-Seidel and SOR methods</li></ul></li><li>○ Nonlinear Systems<ul style="list-style-type: none"><li>▪ Newton and Quasi-Newton methods</li><li>▪ Steepest descent techniques</li></ul></li></ul></li></ul>	25%

**Student Learning Outcomes (SLO):** At the end of MTH 305, a student who has studied and learned the material should be able to:

1. Recognize circumstances when numeric methods can and should be used. [PLO: 1, 5]
2. Use several basic numeric methods for solving equations of one variable. [PLO: 2, 4]
3. Find polynomial approximations for functions. [PLO: 2, 4]
4. Numerically approximate derivatives and integrals. [PLO: 2, 4]
5. Use methods for solving linear and nonlinear systems of equations. [PLO: 2, 4]
6. Use "current" computer software available for numeric solutions. [PLO: 4]

**Program Learning Outcomes (PLO):**

Students graduating from SFASU with a B.S. degree and a major in mathematics will:

1. Demonstrate comprehension of core mathematical concepts. [**Concepts**]  
(notion of theorem, mathematical proof, logical argument)
2. Execute mathematical procedures accurately, appropriately, and efficiently. [**Skills**]  
(calculus, algebra, routine, nonroutine, applied)
4. Demonstrate competence in using various mathematical tools, including technology, to formulate, represent, and solve problems. [**Problem Solving**]  
(calculus tools, algebra tools, applied tools, nonstandard problem solving)
5. Demonstrate proficiency in communicating mathematics in a format appropriate to expected audiences. [**Communication**]  
(written, visual, oral)